

We survey 100 people and split them up as being or *not* being in sets A, B, and C.  
What more can we learn?

We have talked before of how we can think of the regions in a Venn diagram as distinct areas, labeling each region with the number of elements in that region.

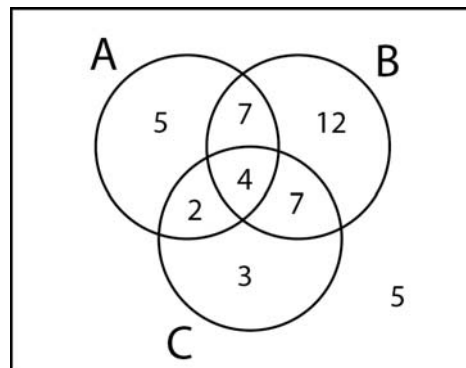
For instance, we have seen this Venn before. Let's put some meaning to it. Let's say that we asked 45 people questions about the music they like.

Let A be the set of people who like country music.

Let B be the set of people who like rock music.

Let C be the set of people who like classical music.

The numbers in each region are the numbers of people in that region. For instance, there are 5 people who like country but neither rock nor classical. Can you mark this region?



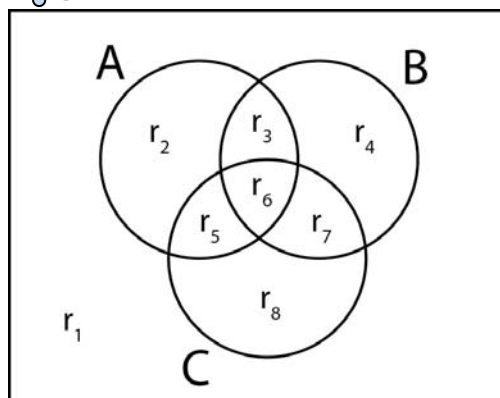
expl 1: For this generic Venn diagram, use set notation to name the regions indicated. There may be more than one answer.

a.)  $r_6$

b.)  $r_6$  and  $r_5$  together

c.)  $r_8$

Generic Venn diagrams will have regions labeled as  $r_1, r_2, r_3$ , etc.



expl 2: For the Venn in the previous example, which regions comprise the set  $C - B$ ?

### Survey Problems:

These problems arise from survey data. Perhaps we asked lots of people questions or delved into existing records. What more can we glean from the information we gather? Here is an example that splits our survey data into two sets.

expl 3: An investigation of auto accidents revealed the following information.

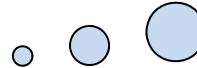
18 accidents involved alcohol and excessive speed

26 accidents involved alcohol

12 accidents involved excessive speed but *not* alcohol

21 accidents involved *neither* alcohol *nor* excessive speed

How many accidents were investigated?

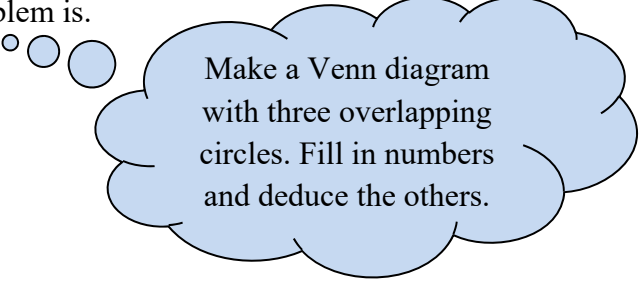


Make a Venn diagram with two overlapping circles. Fill in numbers and deduce the others.

expl 4: From the information below, find the number of elements in the sets A, B, and C. If the data is inconsistent, say so and state where the problem is.

$$A \cap B = \emptyset, \quad n(A \cap C) = 5, \quad n(B \cap C) = 3,$$

$$n(C - A) = 7, \quad n(A - C) = 2, \quad n(U) = 14$$



Make a Venn diagram with three overlapping circles. Fill in numbers and deduce the others.

The **cardinal numbers** of these sets are  $n(A) = \underline{\hspace{2cm}}$ ,  $n(B) = \underline{\hspace{2cm}}$ , and  $n(C) = \underline{\hspace{2cm}}$ .

### **Worksheet: Exploring Venn Diagrams:**

This worksheet will practice the next type of problem. We are given the number of elements in several regions of a Venn and asked to determine the rest.

expl 5: A television network conducted a market survey to determine the evening viewing preferences of people in the 18–25 age bracket. The following information was obtained.

- 3 prefer a reality show early on weekdays
- 14 want to watch TV early on weekdays
- 21 want to see reality shows early
- 8 want reality shows on weekdays
- 31 want to watch TV on weekdays
- 36 want to watch TV early
- 40 want to see reality shows
- 13 prefer late, weekend shows that are *not* reality shows

Describe the sets with which we are working.

Draw a Venn and start by labeling the regions in the middle.

From this information, determine how many people surveyed do *not* want to see reality shows and how many people surveyed prefer to watch TV on the weekend.

So, how many people surveyed do *not* want to see reality shows?

And, how many people surveyed prefer to watch TV on the weekend?