

Solving equations using inverses

NAME: _____

For each function, complete the following steps in the spaces provided.

- Describe the function in words. What we do to an x to get a y ?
- Find the function's inverse. Do not simplify as you go.
- Describe the inverse in words. What we do to an x to get a y ?
- Solve the given equation. Detail the steps as you go. Notice the steps needed are exactly those that the inverse accomplishes.

Solving equations may be easier if you think through them using the idea of inverses and the notion of “unburying the variable”. The first one is done for you. Show as much detail as shown in the example. Make sure you understand each step.

Original function	Find its inverse.	Solve the equation. Write down the steps. Show all work.
$y = 2x + 3$ In words: Start with x , Multiply by 2, Add 3, End y	$y = 2x + 3$ $x = 2y + 3$ $x - 3 = 2y$ $\frac{x-3}{2} = y$ In words: Start with x , Subtract 3, Divide by 2, End y Switch x and y and then solve for y . Notice this undoes the original function.	$7 = 2x + 3$ Subtract 3 $4 = 2x$ Divide by 2 $2 = x$ These steps mimic the inverse's operations.

Original function	Find its inverse.	Solve the equation. Write down the steps. Show all work.
<div data-bbox="191 321 331 394">$y = \frac{3x + 2}{4}$</div> <div data-bbox="191 508 323 540">In words:</div>	<div data-bbox="632 1084 768 1117">In words:</div>	<div data-bbox="1205 321 1346 394">$5 = \frac{3x + 2}{4}$</div>

Original function	Find its inverse.	Solve the equation. Write down the steps. Show all work.
<div data-bbox="191 321 338 402">$y = \sqrt{\frac{x-2}{3}}$</div> <div data-bbox="191 483 323 516">In words:</div>	<div data-bbox="632 1084 768 1117">In words:</div>	<div data-bbox="1205 321 1352 402">$3 = \sqrt{\frac{x-2}{3}}$</div>

Original function	Find its inverse.	Solve the equation. Write down the steps. Show all work.
$y = \frac{2x - 4}{3} + 5$ <p>In words:</p>	<p>In words:</p>	$7 = \frac{2x - 4}{3} + 5$

Original function	Find its inverse.	Solve the equation. Write down the steps. Show all work.
$y = -3\sqrt{x} + 4$ In words:	In words:	$-8 = -3\sqrt{x} + 4$