

The difference between OR and AND

NAME:

When studying probability, we may want to find the probability that event A *and* event B occur at the same time, or the probability that event A *or* event B occurs. We'll need to make some distinctions between OR and AND.

**We'll use AND if we mean both events will occur at the same time.**

**We'll use OR if we mean either one, or the other, or both events will occur. Let's look at some examples.**

The probabilities on this worksheet can be figured simply by calculating

$$\text{Probability of an event} = \frac{\text{number of successes}}{\text{number of total possibilities}}$$

1a.) Consider rolling a six-sided die and tossing a coin. Write down the sample space.

1b.) What is the probability of rolling an even number AND tossing a heads? Write down the successes from the sample space.

1c.) What is the probability of rolling an even number OR tossing a heads? Write down the successes from the sample space.

Consider picking a single card out of a poker deck. A poker deck contains four suits: diamonds, hearts, spades, and clubs. The diamonds and hearts are red and the spades and clubs are black. Each suit has thirteen cards: Ace, 2, 3, 4, 5, 6, 7, 8, 9, 10, Jack, Queen, and King. This makes a total of 52 cards. A face card will be defined to be a Jack, Queen, or King.

2a.) You are interested in the probability of selecting a red Queen. Is this event represented by “red AND Queen” or “red OR Queen”?

2b.) Find the probability of selecting a red Queen. Write down the successes.

2c.) Find the probability that the card selected will be either red OR a Queen. Describe the successes.

2d.) Find the probability that the card selected will be either red OR a Queen, but not both. Describe the successes.

3a.) Consider the experiment of tossing a single coin. What is the probability that I toss heads OR tails? Count the successes and the possibilities. Since the successes include all the possibilities, what will you get for the probability?

3b.) In general, if two events A and B are the only two events that can occur, then  $P(A \text{ or } B)$  is what numerical value? This should be equivalent to the answer you got above. Essentially, I am asking the same thing.

4a.) Consider the experiment of selecting one marble out of a bag with ten marbles: four green, two blue, three yellow, and one red. What is the probability I select a marble that is red AND green? Again, think about how many successes are in the bag. How many marbles are both red and green?

4b.) In general, if two events A and B cannot occur at the same time, then  $P(A \text{ and } B)$  is what numerical value? Again, this should be equivalent to the answer you got above. Essentially, I am asking the same thing. This is a fact that is used quite a lot, called the “probability of two mutually exclusive events”.